

# Development of Concurrent Constraint Languages for multiparadigm programming

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FGCS'94 December 1994

# This Talk

## CCP LANGUAGES

- Basic CCP
- Deep CCP (AKL)
- Higher Order CCP (Oz)
- Integration of Search, Concurrent Objects and Higher Order

Many thanks to fiends from SICS and DFKI,  
specially Sverker Janson and Johan Montelius SICS  
and Gert Smolka and Christian Schulte DFKI

# Concurrent Constraint Programming

- combines ideas from
  - concurrent logic programming
  - constraint logic programming
  - functional programming
  - concurrency theory
- aims at
  - concurrent symbolic programming
  - problem solving with constraints and search
  - combination of the above
  - parallel implementation
  - transparent distribution

# CCP Important developments

## Flat CCP

- FGHC ICOT (Ueda, Chikayama) 1985
- Michael J. Maher. Logic semantics for a class of committed-choice programs. 1987.
- Vijay A. Saraswat. Compositional Syntax, the notion of constraint store, ask and tell operations.
- Yang/Warren/Haridi. Introduction of nondeterminism and global search. The notion of determinism driven execution

## Deep CCP

- Haridi/Janson. AKL (Agents Kernel Lang). Model for guard execution, integration of search and concurrency, the notion of stability, encapsulated search.
- AKL, ports (named streams), essential for integration of concurrent object oriented programming, and encapsulation of mutable state.

## CCP Important developments 2

- Smolka et al, DFKI, Oz. Higher order CCP. Record datatypes, names: subsumes functional programming, modules as special case of usage of records and HO CCP.
- Oz, Cells as simplification of AKL / ports, concurrent object-oriented programming based on prototypes.
- Oz, controlled encapsulated search using the solve combinator. Search is programmable at the user level.

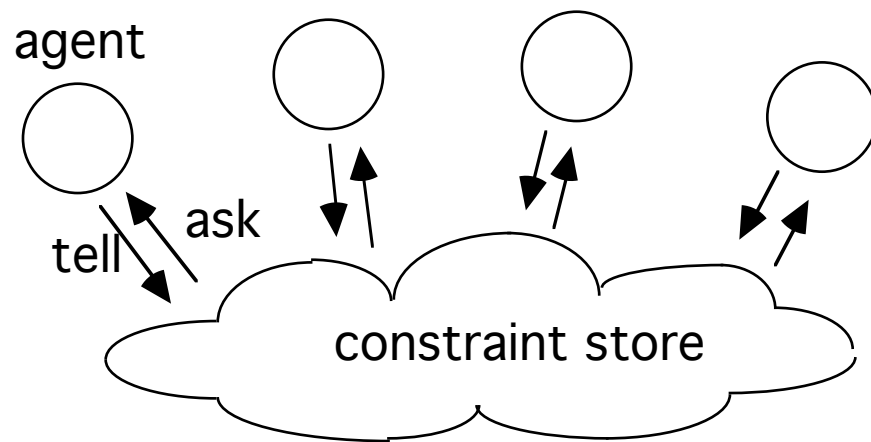
### **Future**

AGENTS II, SICS / DFKI

Adds: Distribution aspects (language for distributed applications)

- persistence, real-time, groups for concurrent exception handling, continuous operation and resource management.
- efficient implementation

## CCP



Agents *tell* constraints to a shared constraint store and may *ask* if constraints are entailed by the store.

## A flat language (cc flavour)

E	::=	$\phi$	<i>constraint</i>
		$p(\mathbf{x})$	<i>call</i>
		$E_1 \ E_2$	<i>composition</i>
		$\mathbf{x} \ \mathbf{in} \ E$	<i>hiding</i>
		<b>or</b> $C_1 \   \ \dots \   \ C_n$ <b>end</b>	<i>disjunction</i>
		<b>if</b> $C_1 \   \ \dots \   \ C_n$ <b>else</b> $E$ <b>end</b>	<i>conditional</i>

C ::=  $\mathbf{x} \ \mathbf{in} \ \phi \rightarrow E$  *clause*

D ::= **proc**  $p(\mathbf{x}) \ E$  **end** *definition*

C **entailed** by  $\psi$  iff  $\psi$  implies  $\exists \mathbf{x} \ \phi$

C **disentailed** by  $\psi$  iff  $\psi$  implies  $\neg \exists \mathbf{x} \ \phi$

## Reduction Rules Flat CCP

- $\phi \Rightarrow$  tell  $\phi$  and halt if store is unsatisfiable
- $E_1 E_2 \Rightarrow E_1 \wedge E_2$
- $\bar{x} \text{ in } E \Rightarrow E[\bar{y} / \bar{x}]$  if  $\bar{y}$  are fresh new variables.
- $p(\bar{y}) \Rightarrow E[\bar{y} / \bar{x}]$  if **proc**  $p(\bar{x}) E$  **end** is in program

**proc** { $p \bar{X}$ }  $E$  **end**

- **if**  $C_1 \mid \dots \mid C_n$  **else**  $E$  **end**  $\Rightarrow \langle C_k \rangle$  if  $C_k$  entailed
- **if**  $C_1 \mid \dots \mid C_n$  **else**  $E$  **end**  $\Rightarrow E$  if  $C_1, \dots, C_n$  disentailed

$\langle \bar{x} \text{ in } \phi \rightarrow E \rangle \equiv \bar{x} \text{ in } (\phi E)$



## Examples

This language is basically KL1 if the domain is trees:

```
proc append(xs, ys, zs)
if   xs = []  $\rightarrow$  zs = ys
  |   x,xr,zr in xs = [x | xr]  $\rightarrow$ 
      zs = [x | zr]
      append(xr,ys,zr)
end
end
```

or in functional notations

```
fun append(xs, ys)
if   xs = []  $\rightarrow$  ys
  |   x,xr in xs = [x | xr]  $\rightarrow$ 
      [x | append(xr,ys)]
end
end
```

## Examples 2

```
proc merge(xs, ys, zs)
  if xs = [] → zs = ys
  | ys = [] → zs = xs
  | x,xr,zr in xs = [x | xr] →
    zs = [x | zr]
    merge(xr,ys,zr)
  | y,yr,zr in ys = [y | yr] →
    zs = [y | zr]
    merge(xs,yr,zr)
end
end
```

## Reduction of Disjunction

**or**  $C_1 \mid \dots \mid C_n$  **end**  $\Rightarrow \langle C_k \rangle$  if

all  $C_i$  different from  $C_k$  are disentailed

```
proc length(xs, n)
or  xs = []  n = 0  $\rightarrow$  true
  |  x, xr, nr in
      xs = [x | xr], n = S(nr)  $\rightarrow$ 
      length(xr, nr)
end
end
```

will be determinacy driven:

$xs = [x1, x2, x3]$  length(xs, n)

produces  $n = S(S(S(0)))$

length(xs, n)  $n = S(S(S(0)))$

produces  $xs = [x1, x2, x3]$

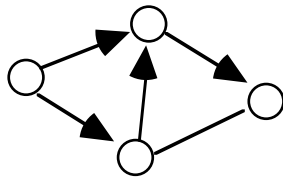
# NONDETERMINISM

or  $C_1 \mid \dots \mid C_n$  end,  $E \Rightarrow$

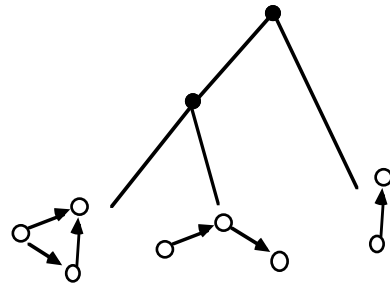
$$(\langle C_1 \rangle \wedge E) \vee \dots \vee (\langle C_n \rangle \wedge E)$$

if no other reduction is possible

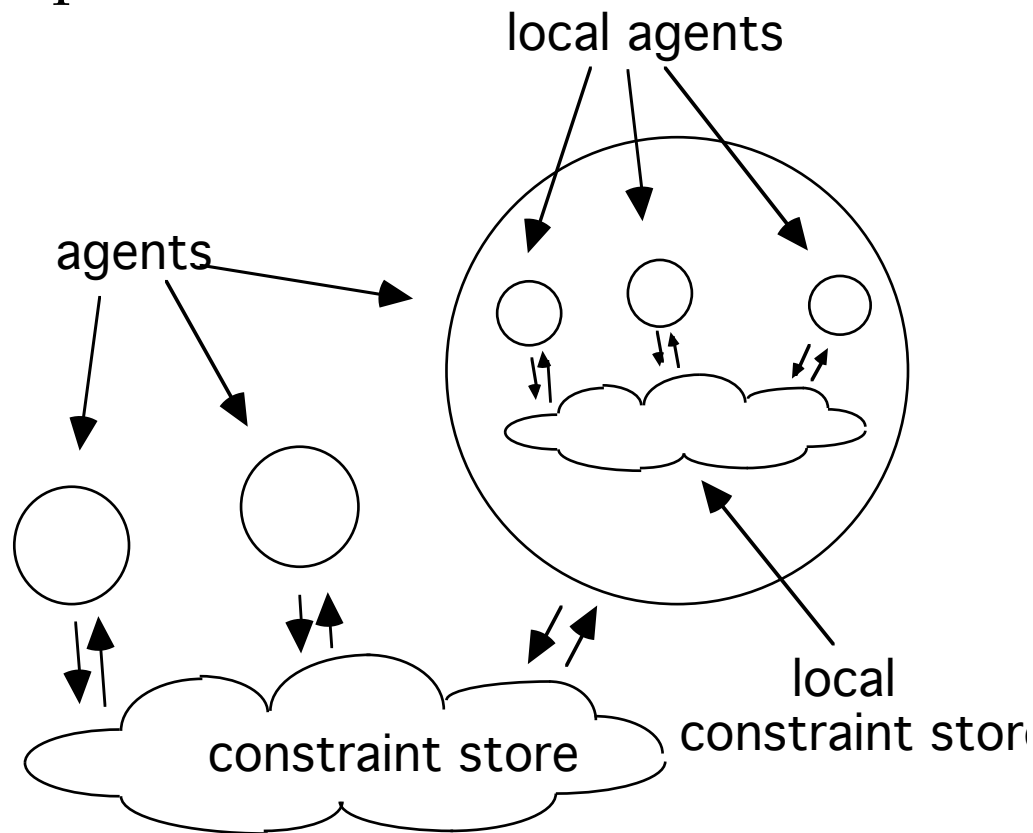
flat+det:



flat+nondet:



## Deep CCP

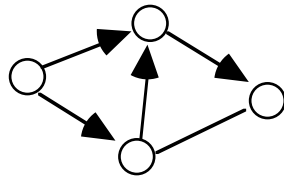


- Local agents see local and external constraints.
- Scope of nondeterminism is local.
- Enables encapsulated search with reactive top-level.
- Supports negation and general conditions.
- The AGENTS implementation of AKL offers record constraints and FD constraints.

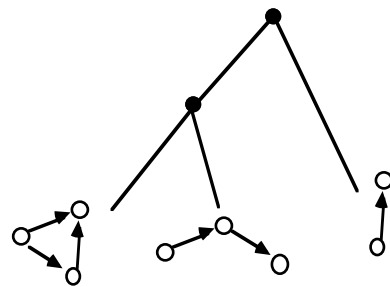
Sverker Janson. *AKL — A Multiparadigm Programming Language*. SICS Dissertation Series 14, Swedish Institute of Computer Science, 1994.

# Flat vs deep

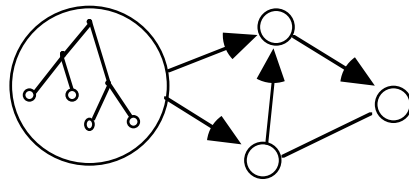
flat+det:



flat+nondet:



deep+nondet:



	"det"	nondet
flat	KL1, Janus, ...	cc, Andorra-I Pandora, ...
deep	CP, GHC, Parlog, ...	AKL, Oz

## Deep CCP (AKL)

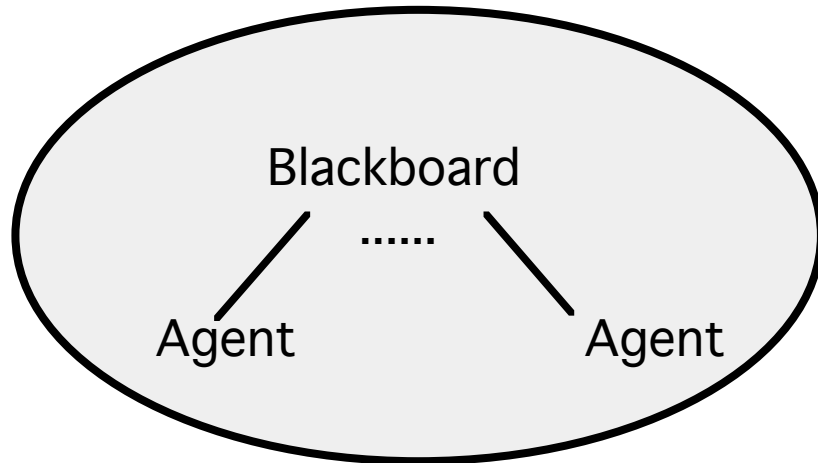
E	::=	$\phi$	<i>constraint</i>
		$p(\bar{x})$	<i>call</i>
		$E_1 \ E_2$	<i>composition</i>
		$\bar{x}$ in E	<i>hiding</i>
		<b>or</b> $C_1$   ...   $C_n$ <b>end</b>	<i>disjunction</i>
		<b>if</b> $C_1$   ...   $C_n$ <b>else</b> E <b>end</b>	<i>conditional</i>
		<b>bagof</b> ( $x, E_1, y$ )	<i>aggregate</i>

C ::=  $\bar{x}$  in  $E_1 \rightarrow E_2$  *clause*

D ::= **proc**  $p(\bar{x})$  E **end** *definition*

**not** E =<sub>def</sub> **if** E **then** false **else** true **end**

# Computation Spaces

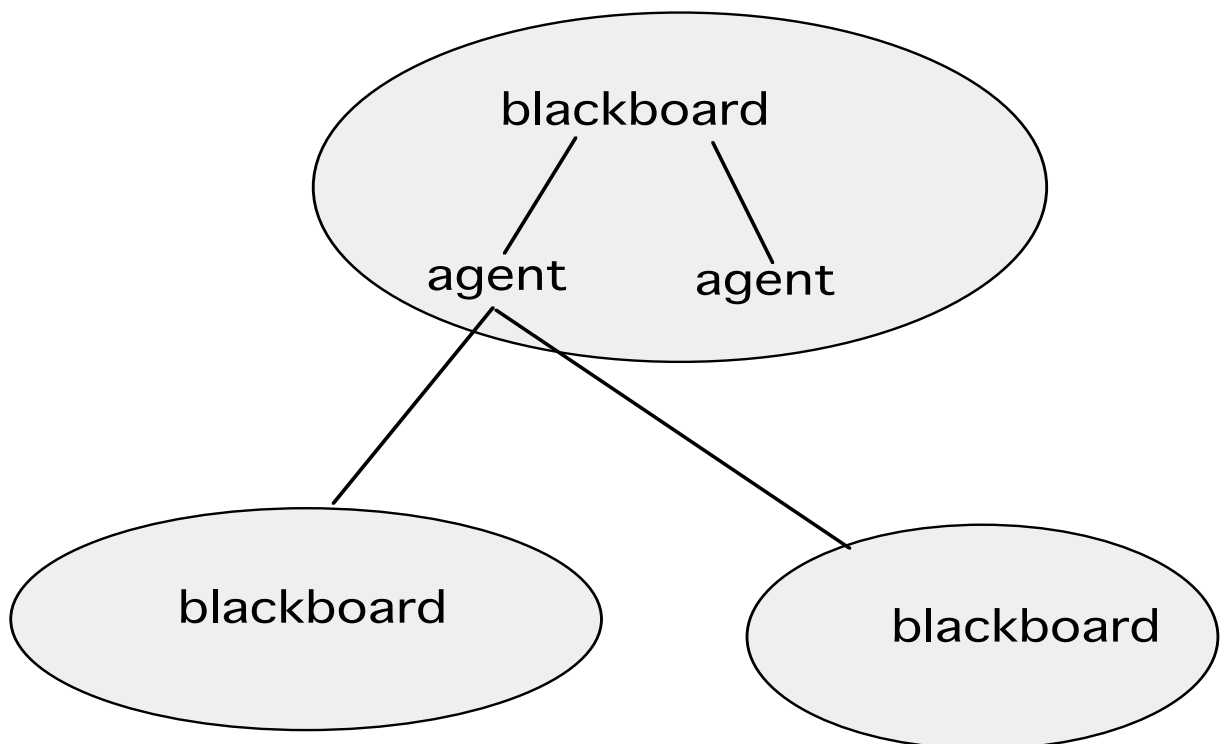


- Blackboard
  - Stores expressions to be executed
  - Stores constraints and local variables
  - Expressions are reduced to constraints
  - Information increases monotonically
- Agents associated with expressions
  - read information from blackboard
  - reduce when sufficient information is available
  - upon reduction might add new constraints and spawn new agents



## Local Computation Spaces

- Agents may have local computation spaces.
- Information local to a local space is invisible outside.
- Information at higher computation spaces are visible to local computation spaces.



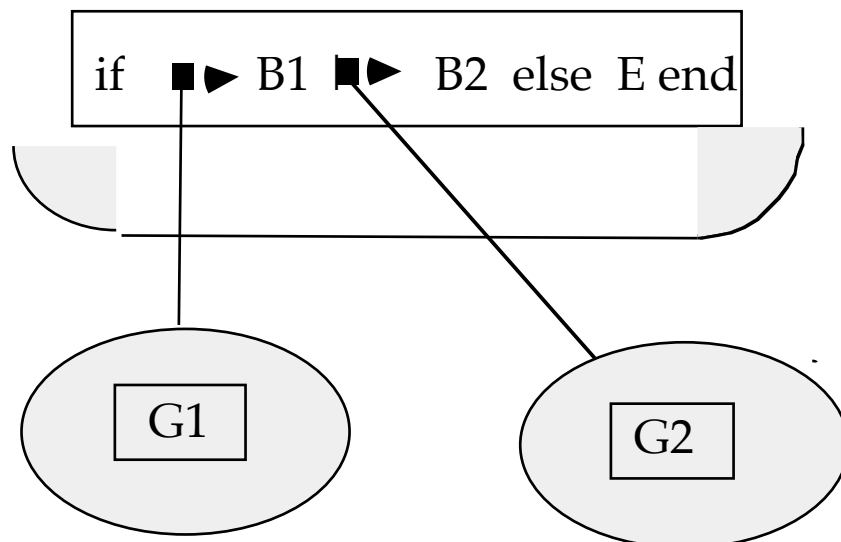
## Semantics 3 (Deep)

Conditional expression:

- **if**  $C_1$  | ... |  $C_n$  **else**  $E$  **end**

where

$C_i ::= X_i$  **in**  $G_i \rightarrow B_i$



- Spawn a local computation space for each  $G_i$
- Suspend the conditional agent
- Start an agent for each  $G_i$

# Stability

An expression  $E$  is *stable* if

For all satisfiable constraints  $\phi$ ,  
 $\phi \wedge E$  is not reducible with 'determinate' rules.

A nondeterminate step is allowed in a stable expression.

NONDETERMINISM (choice splitting)

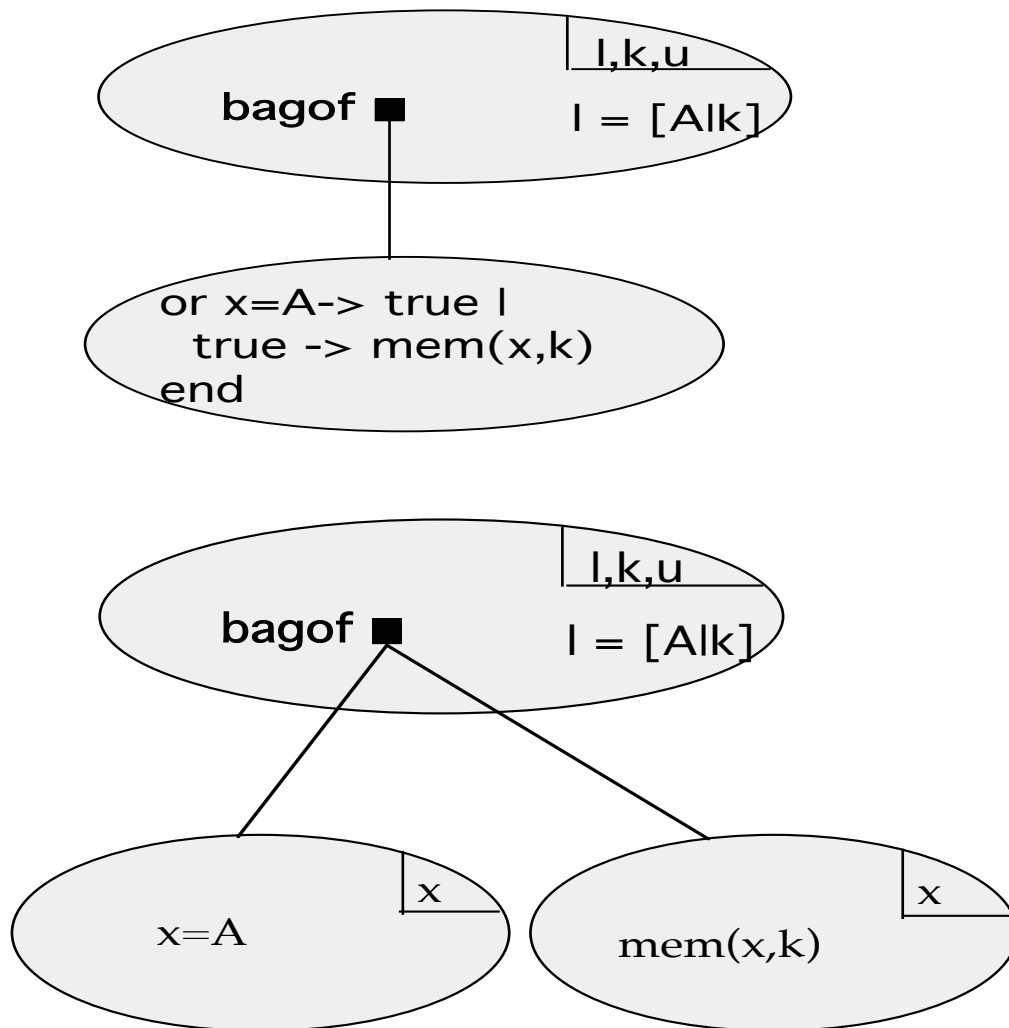
or  $C_1 \mid \dots \mid C_n \mathbf{end}$ ,  $E_r \Rightarrow$

$$(C_1 \wedge E_r) \vee \dots \vee (C_n \wedge E_r)$$

if the computation space is stable

- The computation space is copied into several copies.
- If the top level computation space is used for external communication then it is always unstable and therefore choice splitting is not allowed.

## Example (stability)



$l, u, k$  in `bagof(x, mem(x, l), u)`  $l = [A | k]$

`proc mem(x, l)`

`or l = [x | _] → true`

`| l1 in l = [_ | l1] → mem(x, l1)`

`end`

`end`

## Higher-Order CCP (Oz)

E ::= $\phi$	<i>constraint</i>
<b>proc</b> $y(\bar{x})$ E <b>end</b>	<i>definition</i>
$y(\bar{x})$	<i>call</i>
E <sub>1</sub> E <sub>2</sub>	<i>composition</i>
$\bar{x}$ <b>in</b> E	<i>hiding</i>
<b>or</b> C <sub>1</sub>   ...   C <sub>n</sub> <b>end</b>	<i>disjunction</i>
<b>if</b> C <sub>1</sub>   ...   C <sub>n</sub> <b>else</b> E <b>end</b>	<i>conditional</i>
<b>solve</b> ( $x:E_1, y$ )	<i>solve</i>

C ::=  $\bar{x}$  **in** E<sub>1</sub> → E<sub>2</sub> *clause*

- Subsumes  $\lambda$ -calculus.
- Elegant support for modules and objects.
- Enables exciting new view of search.
- Introduces a the notion of names in addition to variables ( $\gamma$  calculus)

# Higher order (functional) programming

```
fun map(xs, p)
  if   xs = []  $\rightarrow$  []
  |    x,xr in xs = [x | xr]  $\rightarrow$ 
  [p(x) | map(xr, p)]
  end
end
```

- Procedures are first class citizens
- Lexical scoping and local definitions
- Work on partial information (incremental)

## Objects (Ports)

- AKL introduces the notion of ports:

Persistent references (names) to the end of a stream:

### **Basic port operations**

- $\text{new\_port}(port, stream)$

$port$  is a new name associated with  $stream$

- $\text{send}(msg, port)$

appends  $msg$  to the stream associated with  $port$   
reassociate  $port$  with the tail of the stream.

### **Derived port operations**

- $\text{send}(msg, p0, p1)$

$p1$  is bound to  $p0$  after  $msg$  is appended to the stream associated with  $p0$

## Basic object-oriented style:

```
proc object(port)
  local state, stream in
    create_state(state)
    open_port(port, stream)
    obj(stream, state)
end
end

proc obj(ms, state0)
  if msg, mr, s1 in ms = [msg | mr] →
    dispatch(msg, state0, state1)
    obj(mr, state1)
  else true
end
```



## Properties (Ports)

- Objects have unique identifiers given by their associated port.
- Objects are active concurrent entities, e.g. in the sense of actors.
- The state is serialised and is not available to the next message until the dispatch operation is performed.
- State is encapsulated.

## Concurrent Objects (Style)

- class is a record structure its features are the name of messages and its values are the corresponding methods:

Class(msg<sub>1</sub>:method<sub>1</sub>, ... , msg<sub>n</sub>:method<sub>n</sub>)

example

```
Class(Inc:
  proc (msg, s, ns)
    x=s.Val, adjoin(Val:x+1,s,ns)
  end)
```

```
proc object(o, class)
  local
    proc generic_object(str, state)
      local msg, str1, l in
        if str = [msg | str1] →
          label(msg,l)
          (class.l)(msg,state,new_state)
          generic_object(str1, new_state)
        end
      end
    end
  stream, state in
    new_port(o,stream)
    create_state(state,class,o)
    generic_object(stream, state)
  end
end
```

## Object (Sugared Syntax)

```
object counter
  from ur_object
  attrs val with Set(0) end
  meth Set(v) val ← v end
  meth Inc val ← @val + 1 end
  meth Get(v) v ← @val end
end
```

Inc^counter

Inc^counter

# Properties of Object System

- Encapsulated State
  - implementation optimised due to single reference property
- Multiple inheritance / differential
- Method delegation
- Private methods and attributes (due to local names)
- Meta-object protocol
  - constraints on message acceptance can be inherited and / or refined
- Methods
  - as first class objects
  - state threading
  - late binding (default)

# Controlled Encapsulated Search

C. Schulte, G. Smolka, and J. Würtz. Encapsulated Search and Constraint Programming in Oz. In *Principles and Practice of Constraint Programming 1994*.

- Search should not be first principle
- Different strategies should be expressible, including one solution, all solutions, best solution (B&B), and demand driven search
- Problem specification (declarative) and search strategy (operational) should be describable by different programs

## Solve Combinator

**solve(x:E, u) ⇒**

### **Failed**

**solve(x:false, u) ⇒ u=Failed**

### **Solved**

**solve(x:E, u) ⇒ u = Solved(**proc (x) E end**)**

### **Stable**

**solve(x : (**or A | B end** , C), u) ⇒**

**Distributed(**proc (x) A C end, proc(x) B C end**)**

# Depth-First Search

```
proc depth(q, u)
  local v in
    solve(q, v)
    if v = Failed  $\rightarrow$  u = Failed
    | s in v = Solved(s)  $\rightarrow$  u = Solved(s)
    | l,r,v1 in v = Distributed(l,r)  $\rightarrow$ 
      depth(l, v1)
      if v1 = Failed  $\rightarrow$ 
        depth(r, u)
      else u = v1
      end
    end
  end
end
```

## One Solution Search

```
proc one(q, u)
  local v in
    solve(q, v)
    if v = Failed → u = Failed
    | s in v = Solved(s) → u = Solved(s)
    | l,r,v1 in v = Distributed(l,r) →
      if s in one(l, Solved(s)) →
        u = Solved(s)
      | s in one(r, Solved(s)) →
        u = Solved(s)
      else
        u = Failed
      end
    end
  end
end
end
```



## Bagof Aggregate Search (Ordered)

```
proc bagof(q, a)
  local
    proc bagof1(q, u,w)
      local v in
        solve(q, v)
        if v = Failed → u = w
        | s in v = Solved(s) →
          x in s(x), u = [x | w]
        | l,r,m in v = Distributed(l,r) →
          bagof1(l, u, m)
          bagof1(r, m, w)
        end
      end
    end
  in bagof(q, a, [])
end
```

